

OKUN'S LAW: EVIDENCE FOR THE BRAZILIAN ECONOMY

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Abstract

In this article we seek to estimate the Brazilian “Okun’s law” with quarterly data ranging from 1980Q1 until 2013Q3. Considering the typical Okun's relationship, $\Delta u = \alpha - \beta \Delta y$, where “ β ” is the Okun coefficient, we have obtained estimates of β between -0.1878 and -0.2055, such values are similar to those of Italy (-0.21) and greater than the value of Japan (-0.12), but lower than those in countries like the UK (-0.58), USA (-0.52), France (-0.43) and Germany (-0.38); the latter values were estimated by Sogner and Stiassny (2002).

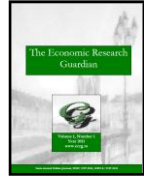
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JEL classification: E23, E24, E27

1. Introduction and literature review

In recent years the Brazilian unemployment rate has experienced a strong decline. In 2002 the unemployment rate was around 12%, while in 2013 the rate was about 5.39%; an average reduction of 0.6 percentage points per year. Between 1981 and 2002 Brazil's GDP grew on average by 2.08% per year.¹ However, if we consider the 2003-2013 period the average growth rate was 3.5% per year. From the neoclassical growth theory, economies tend to grow at a constant rate in the long-run; a rate consistent with a balanced growth path. Apart from issues of convergence, it is expected that the economy average growth is close to the rate consistent with a balanced growth path. If we assume the balanced growth rate of the Brazilian economy was 2.08% per year, then between 2001 and 2013 the economy grew by 1.42 percentage points above the rate of balanced growth path. A quick calculation for the 2002-2013 period shows that for each 1 percentage point that the output grew above the balanced growth rate the unemployment

¹ Between 1981 and 2013 the Brazilian economy grew 2.55% per year on average.



decreased by 0.42 percentage points. This empirical relationship between unemployment variation and output growth is known as Okun's Law.

Okun's law implies an empirical and negative relationship between the change in the unemployment rate and the output growth rate. Proposed by Okun (1962), this relationship has proved robust over time and across countries. Okun's law is a basic building block of traditional macroeconomics models, e.g. the combination between Okun's law and the Phillips Curve is used to derive the aggregate supply relationship (Cuaresma, 2008). Okun's law should be seen as a rule of thumb rather than a "scientific" law because it is not based on a theory. However such rule is useful as a shortcut to more complicated macroeconomic models. The question that Okun wanted to answer in his 1962 paper "Potential GNP: Its measurement and significance", was: "how much output the economy can produce at full employment?" And the answer, according to Okun, was the concept of potential output and its measurement. Potential output for Okun is:

Potential GNP is a supply concept, a measure of productive capacity. But it is not a measure of how much output could be generated by unlimited amounts of aggregate demand. The nation would probably be most productive in the short-run with inflationary pressure pushing the economy. But the social target of maximum production and employment is constrained by a social desire for price stability and free markets. The full employment goal must be understood as striving for maximum production without inflationary pressure... [Okun (1962, p.1)]

In this passage we note that Okun takes account of price stability as a necessary condition for calculation of potential output. This idea anticipates, in a sense, the idea of a NAIRU (non-accelerating inflation rate of unemployment), due to Phelps (1967) and Friedman (1968) as noted by Prachowny (1993, p. 331). Okun's equation is usually written as:

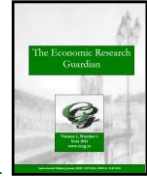
$$\Delta u_t = -\beta(g_y - \bar{g}_y) \quad (1)$$

The β coefficient, sometimes called Okun coefficient, measures how much the unemployment rate varies when the output growth rate (g_y) is different from the potential output growth rate (\bar{g}_y). In their calculations for the U.S., Okun found $\beta \approx 0.30$. But in fact, Okun was interested in the inverse of β , i.e., $1/\beta$, because he wanted to know how much output is "lost" when unemployment is above a certain amount. As $1/\beta \approx 3$, a percentage increase (decrease) in unemployment should result in three point percentage of decrease (increase) in output growth.

The coefficient β in the above equation is affected by variables involved in labor market and production process like labor productivity, hours worked, labor's laws, unions-entrepreneurs relationship, level of firms' capacity utilization, among others things. By the way, Okun's arguments suggest that the empirical link between unemployment and output should not be interpreted in a *ceteris paribus* way, but rather as capturing a simultaneous effect among labor force, hours worked and labor productivity (Cuaresma, 2008). The potential output growth rate, in turn, is an unobserved variable; such variable depends on the labor force growth rate, technical progress, productivity, among other things (Stock and Vogler-Ludwig, 2010).

However, Barreto and Howland (1993) strongly criticize the Okun procedure of use the reciprocal of β to predict the output growth rate associated with a given unemployment rate.²

² Plosser and Schwert (1979) also raised this issue.



According to the authors, the reciprocal of β is a biased³ estimate for the effect of unemployment on the output growth rate. The question is related to what we want to predict. If the intention is to predict the output given the unemployment, so one regresses output on unemployment; if the intent is to predict unemployment given the output, so one regresses the unemployment on output (Barreto and Howland, 1993).

As far as we know there are no studies specifically concerned in getting Okun coefficient values for the Brazilian economy. We believe that the estimate of Okun's law for the Brazilian economy is a necessary contribution to fill a missing topic in the literature about Okun's law. So, our objective in this paper is to estimate the Okun coefficient for the Brazilian economy for comparison with the values obtained in other countries. As now there are more sophisticated procedures for calculating potential output, and in view of the Barreto and Howland (1993) critique, our goal in this paper is focused on regressions of unemployment rate on the output, i.e., how much the unemployment rate varies given the variations in the output growth rate. Of course, ideally the relationship between unemployment and output should be estimated within a system of simultaneous equations involving other theoretically relevant economic variables. But as the "Okun's law" is a rule of thumb often used in practical analyzes and undergraduate textbooks, we estimate such relationship to Brazil for comparison with the values obtained in other countries.

To achieve our goal this paper is divided into four sections besides this introduction: the second section presents estimates of Okun's law to other countries by different methods; in the third section we estimate the Okun's law to Brazil by different methods, and the fourth section concludes.

2. The Okun coefficient in different countries

Moosa (1997) based on Weber (1995), using 1960-1995 annual data for the G7 countries, estimated the following model of the Okun relationship:

$$u_t^c = \alpha + \beta u_{t-1}^c + \gamma y_t^c + \varepsilon_t \quad (2)$$

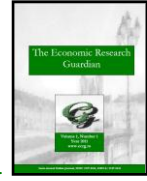
where u_t^c is the unemployment gap, y_t^c is the output gap and ε_t is a random error. The "short term" Okun coefficient in this model is γ , while the "long-term" coefficient is $\theta = \gamma/(1 - \beta)$. The output and unemployment gaps were calculated using state-space models as developed by Harvey (1985, 1989).

Lee (2000) estimated the Okun's coefficient for 16 OECD countries using postwar annual data. He estimated two types of models with the output as the independent variable and unemployment as the dependent variable. The first model is estimated in first differences:

$$\Delta y_t = \beta_0 - \beta_1 \Delta u_t + \varepsilon_t \quad (3)$$

where Δy_t is the difference of the output logs, Δu_t is the variation in the unemployment rate and ε_t is a random error. The second model, in turn, is estimated using the variables gaps:

³ Generally an over-estimate.



$$y_t^c = -\beta_2 u_t^c + \varepsilon_t \tag{4}$$

where y_t^c is the gap of the output log, u_t^c is the unemployment rate gap and ε_t is a random error. The gaps were calculated using the Hodrick-Prescott filter, the Beveridge-Nelson filter and the Kalman filter. Sogner and Stiasny (2002) estimated the Okun relationship for 15 OECD countries using 1960-1999 annual data. The estimated model used a lag in the rate of output growth to capture lags in the employment reaction:

$$\Delta u_t = \alpha_0 + \alpha_1 \Delta y_t + \alpha_2 \Delta y_{t-1} + v_t \tag{5}$$

$$\Delta u_t = \alpha_0 + \alpha_1 \Delta^2 y_t + (\alpha_1 + \alpha_2) \Delta y_{t-1} + v_t \tag{6}$$

where α_1 is the impact effect of output growth rate on the change in unemployment rate, and $(\alpha_1 + \alpha_2)$ is the long-term effect, i.e., the Okun coefficient. Δu_t and Δy_t are respectively the unemployment rate variation and the output log first differences. v_t is a error that can follow an AR (1) process $v_t = \rho v_{t-1} + \varepsilon_t$.

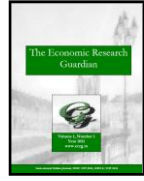
Table 1 shows the estimates obtained for some countries in the studies described above. Japan and Italy are the countries with the lowest estimated coefficients, possibly demonstrating a greater rigidity in labor market in these countries. Germany, France and UK have more similar coefficients with the United States. It is also interesting to compare the estimates of Lee (2000) with those of Moosa (1997) and Sogner and Stiasny (2002).

Table 1: Okun coefficient for selected countries according to different studies

Study	Japan	Italy	Germany	France	USA	UK
Moosa (1997)	-0.088	-0.184	-0.407	-0.363	-0.456	-0.372
Lee (2000)						
First Differences	-0.227	-0.917	-0.405	-0.344	-0.543	-0.719
Kalman Filter	-0.079	-	-0.581	-0.400	-0.532	-0.671
Hodrick-Prescott	0.153	-1.754	-0.459	-0.455	-0.478	-0.709
Beveridge-Nelson	-0.182	-0,415	-0,565	-0,344	-0,493	-0,662
Sogner e Stiasny (2002)	-0.12	-0.21	-0.38	-0.43	-0.52	-0.58

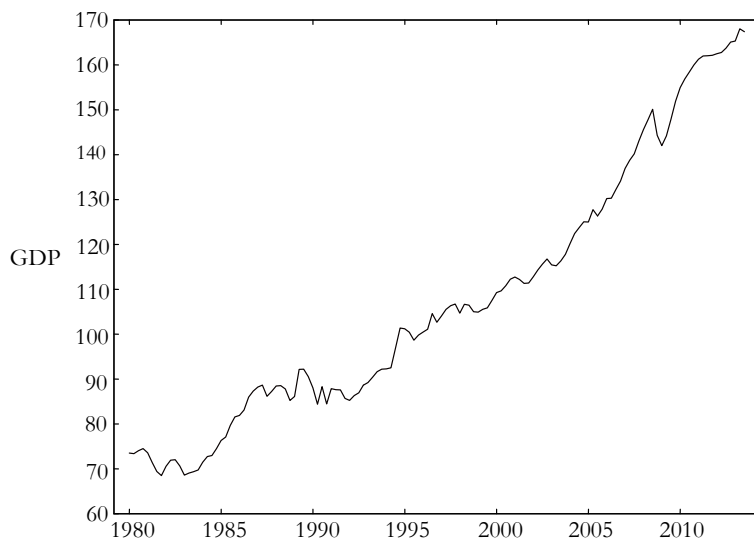
Source: Stock and Vogler-Ludwig (2010, p. 27).

Lee, unlike the other two authors, estimated an output versus unemployment model and therefore estimated a reversed Okun coefficient. Recalling the Barreto and Howland (1993) criticism on the bias involved in using the reciprocal of the Okun coefficient to predict the output growth rate, one note that the coefficients obtained by Lee are higher than those obtained by the two other authors, mainly to Japan and Italy. Again the question is what one wants to predict. If the intention is to predict the output given the unemployment, then the Lee specification is the correct one, on the other hand, if the intent is to predict unemployment given the output, then the specification of Moosa (1997) and Sogner and Stiasny (2002) is the correct one.



3. Estimates for Brazil

The GDP data used in our estimates covers the 1980Q1-2013Q4 period and is provided by the Brazilian Institute of Geography and Statistics (IBGE). The quarterly GDP is seasonally adjusted by the package X12-ARIMA version 0.3 installed on econometric software Gretl 1.9.10.⁴ The graph of GDP is plotted in Figure 1.



Source: Brazilian Institute of Geography and Statistics (IBGE).

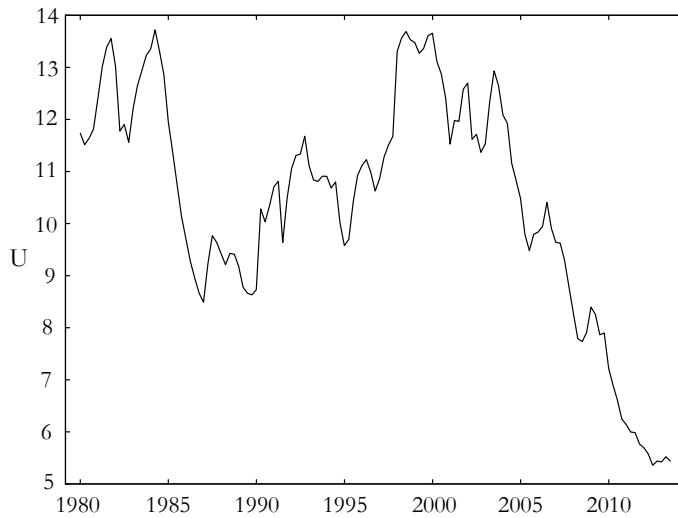
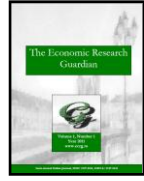
Note: Average of 1995 = 100.

Figure 1 - Seasonally adjusted quarterly Brazilian GDP: 1980Q1-2013Q3

The unemployment rate used comes from the Monthly Employment Survey (PME) of IBGE. The PME began to be held in 1980 and suffered a methodological change in March 2002. Among other changes, the major one was the minimum age of the working age population. Until February 2002, it was considered persons aged 10 or older, from March 2002 the survey has considered only those with 15 years or more of age. The two surveys were collected by IBGE between March 2002 and December 2002 in order to compare the results.

In the old methodology, the unemployment rate in March 2002 was 7.76%, in the same month this rate was 12.93% by the new methodology, 5.17 percentage points higher. In order to chain the two series, we add to every unemployment rate prior to March 2002, 5.17 percentage points. Thus the rate of February 2002 increased from 7.79% to 12.96%, the rate in January 2002 rose from 7.51% to 12.68% and so on until January 1980.

⁴ Cottrell and Lucchetti (2014)



Source: Brazilian Institute of Geography and Statistics (IBGE).

Note: seasonal adjustment of the weighted average of the monthly rates.

Figure 2 - Seasonally adjusted quarterly Brazilian unemployment rate: 1980Q1-2013Q3

The aggregation of the monthly unemployment rates in quarterly rates was done by a weighted average of monthly rates according to the formula:

$$u_t^T = \frac{\sum_{i=1}^3 (u_{iq}^M)^2}{\sum_{i=1}^3 u_{iq}^M} \quad (7)$$

where u_t^Q is the quarterly unemployment rate in quarter q, and u_{iq}^M is the monthly unemployment rate in month i of quarter Q. For example, in January, February and March 1980 unemployment rates were, respectively, 12.48, 12.35 and 12.41%; so the unemployment rate in the first quarter of 1980 was:

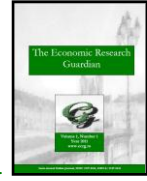
$$u_1 = \frac{(12.48)^2 + (12.35)^2 + (12.41)^2}{12.48 + 12.35 + 12.41} \approx 12.41 \quad (8)$$

and so it was done for the other quarters. These unemployment rates were seasonally adjusted by the X12-ARIMA version 0.3 package installed on econometric software Gretl 1.9.10. The graph of unemployment is plotted in Figure 2.

Using data from the quarterly GDP and the quarterly rate of unemployment, both properly seasonally adjusted, we proceeded to estimate the Okun relationship to Brazil. Since potential output \bar{g}_y is an unobserved variable, the empirical Okun relationship is obtained running the following ordinary least squares (OLS) regression:

$$\Delta u_t = -\beta(g_{y_t} - \bar{g}_y) \quad (9)$$

$$\Delta u_t = \alpha - \beta g_{y_t} + \varepsilon_t \quad (10)$$



where Δu_t is the difference in the unemployment rate, $\alpha = \beta \bar{g}_y$, g_{y_t} is the GDP growth rate in %, and ε_t is a random error. The results of the model (10) are shown in Table 2.⁵ The estimated β coefficient around -0.116514 is low by international standards. The intercept is statistically insignificant. However, the residuals diagnostics indicates the presence of residual autocorrelation. The maximum likelihood estimate shown in Table 3 produces a β coefficient around -0.091595, somewhat smaller than the one estimated in Table 2. In Table 3, the intercept is also statistically insignificant.

Table 2: OLS Estimates of Okun's Law for Brazil (Model 10) – 1980Q2-2013Q3

		Coefficient	Standard-Error ¹	t-ratio	p-value
Constant	α	0.0265338	0.0416056	0.6377	0.5247
g_y	β	-0.1165140	0.0206797	-5.6340	1.02e-07 ***
Obs. 134	$R^2 = 0.2014$	$F(1,132) = 31.74$	$\rho = 0.1393$		Durbin-Watson = 1.72

Residuals and Model Diagnostics

Test Object	Test	Null Hypothesis	Test statistic	P-value
Normality	Jarque-Bera: $Qui^2(2)$	normal residuals	5.3206	0.069
1 st order Autocorrel.	Durbin-Watson	no autocorrelation	1.7173	0.0486
9 th order Autocorrel.	LM of Breusch-Godfrey	no autocorrelation	2.3698	0.0166
Heteroskedasticity	LM of White: $Qui^2(2)$	no heteroskedasticity	2.6936	0.2601
Heteroskedasticity	LM of Breusch-Pagan	no heteroskedasticity	1.4269	0.2323
4 th order ARCH	LM	no ARCH effect	0.6473	0.9577
Parameters stability	CUSUM	parameters stability	-0.2408	0.8102

Source: Prepared by authors.

¹Note: Standard errors robust to heteroskedasticity (HAC).

Table 3: Maximum Likelihood Estimation of Okun's Law to Brazil (Model 10) – 1980Q2-2013Q3

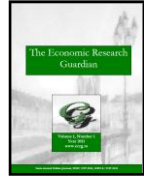
		Coefficient	Standard-Error	z-ratio	p-value
Constant	α	-0.001608	0.030956	-0.0519	0.9586
g_y	β	-0.090409	0.018523	-4.8800	1.06e-06 ***
Dummy 1998 T1		1.283000	0.322546	3.8580	0.0001 ***
	ε_{t-1}	0.135207	0.086266	1.5670	0.1170
	ε_{t-2}	0.095552	0.095712	0.9983	0.3181
	ε_{t-3}	0.174939	0.078360	2.2320	0.0256 **
	ε_{t-4}	-0.275359	0.090958	-3.0270	0.0025 ***
	ε_{t-5}	-0.224781	0.079192	-2.8380	0.0045 **

Residuals and Model Diagnostics

Test Object	Test	Null Hypothesis	Test statistic	P-value
Normality	Jarque-Bera: $Qui^2(2)$	normal residuals	2.8154	0.2447
6 th order autocorrel.	LM de Breusch-Godfrey	no autocorrelation	0.6787	0.4100
4 th order ARCH	LM	no ARCH effect	0.9593	0.9159

Source: Prepared by authors.

⁵ The models estimated in this paper have used the econometric software GNU Gretl 1.9.10.



One reason for the low coefficient β obtained can be the fact that the relationship between changes in the unemployment rate and the GDP growth rate involves some sort of lag. As shown above, Sogner and Stiassny (2002) proposed the following specification:

$$\Delta u_t = \alpha_0 + \alpha_1 g_{y_t} + \alpha_2 g_{y_{t-1}} + v_t \quad (11)$$

$$\Delta u_t = \alpha_0 + \alpha_1 \Delta g_{y_t} + (\alpha_1 + \alpha_2) g_{y_{t-1}} + v_t \quad (12)$$

The coefficient α_1 is the impact coefficient, and $(\alpha_1 + \alpha_2)$ is the effect coefficient, i.e., the Okun coefficient itself. The estimative by Cochrane-Orcutt Method of the model (12) is shown in Table 4.

Table 4: Estimate of Okun's Law to Brazil using the specification of Sogner and Stiassny (2002) and applying the Cochrane-Orcutt Method (Model 12) – 1980Q3-2013Q3

		Coefficient	Standard-Error	t-ratio	p-value	
Constant	α_0	0.073551	0.0389697	1.887	0.0614	*
Δg_v	α_1	-0.097106	0.0170404	-5.699	8.00e-08	***
g_{v-1}	$(\alpha_1 + \alpha_2)$	-0.187770	0.0244486	-7.68	3.73e-012	***
Dummy	1991 Q3	-1.426380	0.3348050	-4.26	3.94e-05	***
Dummy	1998 Q1	1.344270	0.3371870	25.00	4.29e-051	***
Obs. 133	$R^2 = 0.4715$	$F(4,128) = 24.29$	$\rho = -0.01$	Durbin-Watson = 2.02		
Residuals and Model Diagnostics						
Test Object	Test	Null Hypothesis	Test statistic	P-value		
Normality	Jarque-Bera: $Qui^2(2)$	normal residuals	0,0469	0,9768		
4 th Order ARCH	LM	no ARCH effect	1,0892	0,8960		

Source: Prepared by authors.

The value estimated to coefficient α_1 was -0.0971064, a value close to the Okun's coefficient estimated in Model (10). The value of $(\alpha_1 + \alpha_2)$ estimated in model (12) was -0.18777, such number is closer to the value of international estimates. If we look at Table 2, we see that this value (-0.18777) is similar to the value obtained for Italy (-0.21) by Sogner and Stiassny (2002) in a model with the same specification of equation (12) above.

A second method used to estimate the long-term version of Okun's coefficient was proposed by Gordon (1984). This method consists of the following distributed lag model:

$$\Delta u_t = \gamma_0 + \sum_{i=1}^k \gamma_{1i} \Delta u_{t-i} + \sum_{i=0}^k \gamma_{2i} g_{y_{t-i}} + \varepsilon_t \quad (13)$$

The estimated long-term version of Okun's coefficient is:

$$u_t = \theta_0 + \theta_1 g_{y_t} + \vartheta_t \quad (14)$$

where $\theta_0 = \Delta \bar{u}_t - \theta_1 \bar{g}_{y_t}$, $\theta_1 = \sum_{i=0}^k \gamma_{2i} / (1 - \sum_{i=1}^k \gamma_{1i})$ the variable indicates the mean of the variable. and $\vartheta_t = \Delta u_t - \theta_0 - \theta_1 g_{y_t}$. The bar above the variable indicates the mean of the variable. The estimated model (13) is shown in Table 5.

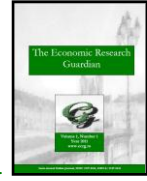


Table 5: OLS estimate of Okun's Law to Brazil using the specification of Gordon (1984) (Model 13) – 1980Q3-2013Q3¹

		Coefficient	Standard-Error ¹	t-ratio	p-value	
Constant	γ_0	0.0738787	0.0361453	2.08290	0.03927	**
Δu_{t-i}	γ_{11}	0.1279210	0.0671094	1.90600	0.05890	*
g_{y_t}	γ_{21}	-0.0993935	0.0177955	-6.10450	1.35e-07	***
$g_{y_{t-1}}$	γ_{22}	-0.0797903	0.0178404	-4.38790	1.70e-05	***
Dummy 1991 T3		-1.2851000	0.0374830	-31.4629	4.74e-066	***
Dummy 1998 T1		1.3783800	0.0545830	26.7440	2.38e-051	***
Obs. 133	$R^2 = 0.4705$	$F(5,127) = 3.40e+19$		$\rho = 0.0207$		h of Durbin = 0.37

Residuals and Model Diagnostics

Test Object	Test	Null Hypothesis	Test statistic	P-value
Normality	Jarque-Bera: $Qui^2(2)$	normal residuals	0.1099	0.9468
1 st Order Autocorrel.	Durbin-Watson	no autocorrelation	1.6623	0.3924
4 th Order Autocorrel.	LM de Breusch- Godfrey	no autocorrelation	0.8292	0.5090
Heteroskedasticity	LM de White: $Qui^2(2)$	no heteroskedasticity	7.9857	0.7146
Heteroskedasticity	LM de Breusch-Pagan	no heteroskedasticity	1.8788	0.8657
4 th Order ARCH	LM	no ARCH effect	0.5419	0.9693
Parameters stability	CUSUM	parameters stability	-0.0400	0.9681

Source: Prepared by authors.

¹Note: Standard errors robust to heteroskedasticity (HAC).

Based on the estimated model (13) we can calculate the long-term version of Okun's coefficient described in equation (14):

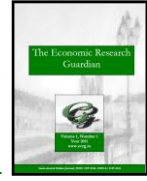
$$\begin{array}{rcl}
 \Delta u_t & = & 0.0819 - 1.4736 \text{ d1991Q3} + 1.5806 \text{ d1998Q1} - 0.2055 g_{y_t} \\
 t & & (2.12) \quad (-3.53) \quad (3.76) \quad (-9.90) \\
 p & & 0.1015 \quad 0.0242 \quad 0.0198 \quad 0.0006 \\
 pb & & 0.1873 \quad 0.0000 \quad 0.0000 \quad 0.0000
 \end{array} \quad (15)$$

$$R^2 = 0.8079 \quad \text{obs.} = 134 (1980:2 - 2013:3)$$

where t is the t-ratio, p is the p-value and pb is the p-value calculated by bootstrap with 10,000 replications.

Again the Okun's coefficient estimated around 0.2055 is plausible and in accordance with estimates to other countries. A look at Table 1 shows that this value is similar to estimates for Italy and Japan, but this value is about half of the estimates to other countries like USA, UK and Germany. This fact may indicate that the Brazilian labor market, as well as Japanese and Italian, is more rigid than the American, German, etc.

However, we must carefully consider these estimates because of the nature of the data used. We use quarterly GDP and unemployment rate for 1980Q1-2013Q3 period, but the unemployment rate refers only to some regions of the country. The unemployment rate used was published by Monthly Employment Survey (PME) by Brazilian Institute of Geography and Statistics (IBGE). PME is conducted monthly in six metropolitan areas (Recife, Salvador, Belo Horizonte, of Rio de Janeiro, São Paulo and Porto Alegre), the sum of the economically active population (EAP) in



these regions is about 25% of the Brazilian EAP. The GDP share of these metropolitan regions on Brazilian GDP was about 33% at the end of the 2000s, i.e., these metropolitan regions produce about one-third of Brazil's GDP and employ about a quarter of Brazilian EAP.

4. Conclusions

In this article our objective was to estimate the "Okun's law" to Brazil with 1980-2013 quarterly data. Whereas the typical specification of Okun's law is $\Delta u_t = \alpha - \beta g_y$, where β is the coefficient of Okun, we obtained estimates of β between -0.1878 and -0.2055, such values are similar to those of Italy (-0.21) and greater than the value of Japan (-0.12), but lower than those in countries like the UK (-0.58), USA (-0.52), France (-0.43) and Germany (-0.38).⁶

In the introduction of this paper, we have mentioned that the Brazilian unemployment rate experienced a strong decline since the early 2000s; such rate stood around 12% in 2002 and fell to 5.39% in 2013 - an average reduction of 0.6 percentage point per year. Assuming a growth rate of potential output around 2.08%, then the output grew by about 1.42 percentage point above potential between 2002 and 2013. The ratio (0.6/1.42) implies an Okun's coefficient of 0.42 for the 2002-2013 period. However in the 1980-2013 period the Okun's coefficient estimates were around 0.20 and regressions analysis do not indicate the presence of structural breaks within this period. Thus the strong reduction in Brazilian unemployment observed in the 2000s must have other causes besides the increase in output growth. One possible explanation may be the reduction in the growth of the working age population observed in Brazil recently. This reduction is a result of the demographic transition experienced by the country in the beginning of the century XXI. How the unemployment rate cannot fall without bound, it's clear that a high output growth rate can only be maintained through a high labor productivity growth. This is the challenge to the Brazilian economy now.

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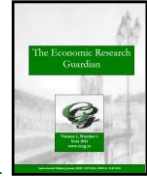
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